Example 1: Consider the graph $f(x)$ shown below:


Relative Max at: $x=$ $\qquad$ ; Relative Min at $x=$ $\qquad$
Absolute Max at: $x=$ $\qquad$ ; Absolute Min at $x=$ $\qquad$
Critical points at: $x=$ $\qquad$ ; $f^{\prime \prime}(x)=0$ at: $x=$ $\qquad$
$f^{\prime}(x)=0$ at: $\quad x=$ $\qquad$
$f^{\prime}(x)>0$ at the interval of: $\qquad$ ; $f^{\prime}(x)<0$ at the interval of: $\qquad$
$f^{\prime \prime}(x)>0$ at the interval of: $\qquad$ ; $f^{\prime \prime}(x)<0$ at the interval of: $\qquad$
$f^{\prime \prime}(x)>0 \& f^{\prime}(x)=0$ at : $x=$ $\qquad$ ; $f^{\prime \prime}(x)<0 \& f^{\prime}(x)=0$ at : $x=$ $\qquad$

Example 2: Consider the graph $f(x)$ shown below:


## Answers:

Please ask your instructor if you don't agree with an answer, you might be correct

## Example 1:

Relative Max at: $x=d$
Relative Min at $x=b$
Absolute Max at: $x=a$
Absolute Min at $x=f$
Critical points or: $\quad f^{\prime}(x)=0$ at: $x=b, d$
$f^{\prime \prime}(x)=0$ (Inflection points) at: $x=c, e$
$f^{\prime}(x)=0$ (Tangent line is horizontal) at: $\quad x=b, d$
$f^{\prime}(x)>0$ (Increasing) at the interval of: $(b<x<d)$
$f^{\prime}(x)<0$ (Decreasing) at the interval of: $(a<x<b)$ and $(d<x<f)$
$f^{\prime \prime}(x)>0$ (Concave Up) at the interval of: $(a<x<c)$ and $(e<x<f)$
$f^{\prime \prime}(x)<0$ (Concave Down) at the interval of: $(c<x<e)$
$f^{\prime \prime}(x)>0 \& f^{\prime}(x)=0$ at (local Minimum) : $x=b$
$f^{\prime \prime}(x)<0 \& f^{\prime}(x)=0$ at (local Maximum) : $x=d$

## Example 2:

|  | $f$ is: $(+, 0,-)$ | $f^{\prime}$ is $:(+, 0,-)$ | $f^{\prime \prime}$ is: $(+, 0,-)$ |
| :---: | :---: | :---: | :---: |
| $\boldsymbol{a}$ | 0 | 0 | + |
| $\boldsymbol{b}$ | + | + | + |
| $\boldsymbol{c}$ | + | 0 | - |
| $\boldsymbol{d}$ | + | 0 | 0 |
| $\boldsymbol{e}$ | + | - | - |
| $\boldsymbol{f}$ | - | - | + |

