[1]


| Corner <br> Points | Function Values: $\mathrm{F}(x, y)=2 x+3 y$ |
| :---: | :--- |
| $(0,2)$ | $\mathrm{F}(0,2)=2(0)+3(2)=6$ |
| $(2,2)$ | $\mathrm{F}(2,2)=2(2)+3(2)=10$ |
| $(-4 / 3,-2 / 3)$ | $\mathrm{F}(-4 / 3-2 / 3)=2(-4 / 3)+3(-2 / 3)=-14 / 3$ |
| $(2,1)$ | $\mathrm{F}(2,1)=2(2)+3(1)=7$ |

Therefore, the maximum value of F is 10 when $\mathrm{x}=2$ and $y=2$, and the minimum value of $F$ is $-14 / 3$ when $x=-4 / 3$ and $y=-2 / 3$.
[3]

[5]


| Corner <br> Points | Function Values: $\mathrm{P}(x, y)=16 x-2 y+40$ |  |
| :---: | :--- | :--- |
| $(0,0)$ | $\mathrm{P}(0,0) \quad=16(0)-2(0)+40=40$ |  |
| $(0,4)$ | $\mathrm{P}(0,4)$ | $=16(0)-2(4)+40=32$ |
| $(8 / 3,4)$ | $\mathrm{P}(8 / 3,4)=16(8 / 3)-2(4)+40=224 / 3$ |  |
|  | $\approx 74.67$ |  |
| $(7,3 / 4)$ | $\mathrm{P}(7,3 / 4)=16(7)-2(3 / 4)+40=301 / 2$ |  |
|  | $=150.5$ |  |
| $(7,0)$ | $\mathrm{P}(7,0)=16(7)-2(0)+40=152$ |  |

Therefore, the maximum value of P is 152 when $x=7$ and $y=0$, and the minimum value of $P$ is 32 when $\mathrm{x}=0$ and $\mathrm{y}=4$.


| Corner <br> Points | Function Values: $\mathrm{F}(x, y)=x+2 y$ |
| :--- | :--- |
| $(0,0)$ | $\mathrm{F}(0,0)=(0)+2(0)=0$ |
| $(0,5)$ | $\mathrm{F}(0,5)=(0)+2(5)=10$ |
| $(1,5)$ | $\mathrm{F}(1,5)=(1)+2(5)=11$ |
| $(6,0)$ | $\mathrm{F}(6,0)=(6)+2(0)=6$ |

Therefore, the maximum value of F is 11 when $\mathrm{x}=1$ and $\mathrm{y}=5$.

| Corner <br> Points | Function Values: $f(x, y)=5 x+4 y$ |
| :---: | :---: |
| $(0,0)$ | $f(0,0)=5(0)+4(0)=0$ |
| $(0,5)$ | $f(0,5)=5(0)+4(5)=20$ |
| $(2,3)$ | $f(2,3)=5(2)+4(3)=22$ |
| $(4,0)$ | $f(4,0)=5(4)+4(0)=20$ |

Therefore, the maximum value of $f$ is 22 when $\mathrm{x}=2$ and $\mathrm{y}=3$.

| Corner <br> Points | Function Values: $\mathrm{G}(x, y)=3 x+4 y$ |
| :--- | :--- |
| $(0,0)$ | $\mathrm{G}(0,0)=3(0)+4(0)=0$ |
| $(0,7)$ | $\mathrm{G}(0,7)=3(0)+4(7)=28$ |
| $(2,6)$ | $\mathrm{G}(2,6)=3(2)+4(6)=30$ |
| $(5,2)$ | $\mathrm{G}(5,2)=3(5)+4(2)=23$ |
| $(6,0)$ | $\mathrm{G}(6,0)=3(6)+4(0)=18$ |

Therefore, the maximum value of G is 30 when $\mathrm{x}=2$ and $\mathrm{y}=6$.


| Corner <br> Points | Function Values: $\mathrm{Z}(u, v)=3 u+4 v$ |
| :---: | :--- |
| $(0,9)$ | $\mathrm{Z}(0,9)=3(0)+4(9)=36$ |
| $(1,6)$ | $\mathrm{Z}(1,6)=3(1)+4(6)=27$ |
| $(5,2)$ | $\mathrm{Z}(5,2)=3(5)+4(2)=23$ |
| $(6,1)$ | $\mathrm{Z}(6,1)=3(6)+4(1)=22$ |
| $(8,0)$ | $\mathrm{Z}(8,0)=3(8)+4(0)=24$ |

Therefore, the minimum value of Z is 22 when $\mathrm{u}=6$ and $\mathrm{v}=1$.
[15]


| Corner <br> Points | Function Values: $\mathrm{A}(a, b)=2 a+5 b$ |
| :---: | :--- |
| $(0,9)$ | $\mathrm{A}(0,9)=2(0)+5(9)=45$ |
| $(2,5)$ | $\mathrm{A}(2,5)=2(2)+5(5)=29$ |
| $(5,1)$ | $\mathrm{A}(5,1)=2(5)+5(1)=15$ |
| $(8,0)$ | $\mathrm{A}(8,0)=2(8)+5(0)=16$ |

Therefore, the minimum value of A is 15 when $\mathrm{a}=5$ and $\mathrm{b}=1$.
[17]


| Corner <br> Points | Function Values: $f(x, y)=x-y$ |
| :---: | :--- |
| $(0,-2)$ | $f(0,-2)=(0)-(-2)=2$ |
| $(0,3)$ | $f(0,3)=(0)-(3)=-3$ |
| $(5,1 / 2)$ | $f(5,1 / 2)=(5)-(1 / 2)=9 / 2$ |
| $=4.5$ |  |$|$|  |  |
| ---: | :--- |
| $(5,-2)$ | $f(5,-2)=(5)-(-2)=7$ |

Therefore, the maximum value of $f$ is 7 when $\mathrm{x}=5$ and $\mathrm{y}=-2$, and the minimum value of $f$ is -3 when $\mathrm{x}=0$ and $\mathrm{y}=3$.

\(\left.$$
\begin{array}{|c|c|}\hline \begin{array}{c}\text { Corner } \\
\text { Points }\end{array}
$$ \& Function Values: f(x, y)=x-y \\
\hline(-3,-7 / 2) \& f(-3,-7 / 2)=(-3)-(-7 / 2)=1 / 2 \\

=0.5\end{array}\right]\)| $(-3,0)$ | $f(-3,0)=(-3)-(0)=-3$ |
| ---: | ---: |
| $(1 / 6,19 / 2)$ | $f(1 / 6,19 / 2)=(1 / 6)-(19 / 2)=-28 / 3$ |
|  | $\approx-9.33$ |
| $(24 / 7,-2 / 7)$ | $f(24 / 7,-2 / 7)=(24 / 7)-(-2 / 7)=26 / 7$ |
|  | $\approx 3.71$ |

Therefore, the maximum value of $f$ is 26/7 (or 3.71) when $x=24 / 7$ and $y=-2 / 7$, and the minimum value of $f$ is $-28 / 3$ (or -9.33 ) when $\mathrm{x}=1 / 6$ and $\mathrm{y}=19 / 2$.

