## SYLLABUS FOR STAT 52800 SPRING 2024 INTRODUCTION TO MATHEMATICAL STATISTICS

Instructor Sean Peng Class Time 4:30–5:45PM MW Office Hours 10:30–11:30AM MW (or by appt/zoom) Math Ph 317-274-6918 E-mail hanxpeng@iu.edu

Dept of Math Sciences Class Room IT 162 Office LD 224B Office Ph 317-274-8070 Zoom ID/Pass 850 0735 8567/446326

Prerequisite STAT 51900 (Introduction to Probability).

Course Description Students will learn the basic concepts of mathematical statistics including sufficiency and completeness, the exponential family of distributions, theory of point estimation, Cramer-Rao inequality, Rao-Blackwell Theorem with applications, maximum likelihood estimation, asymptotic distributions of maximum likelihood estimators, hypothesis testing, Neyman-Pearson Lemma, UMP tests, generalized likelihood ratio test, asymptotic distribution of the GLR test, and sequential probability ratio test. The prerequisite of this course is STAT 51900. It is suitable for students in mathematics, economics, business etc. who do not wish to pursue a program in statistics. However, it is a required course for statistics masters, mathematical statistics and biostatistics PhD programs, and so we will focus on concepts that are essential for statistical/bio-statistical applications. This course prepares you for advanced statistics course STAT 62800.

TEXTBOOK Hogg, McKean and Craig (2005). Introduction to Mathematical Statistics, 8th ed. Pearson Education Inc., ISBN 978-0-13-468699-8.

SoS Policy on Technology and Devices Unless stated otherwise by the instructor, cell phones, tablets, computers, smart/electronic/digital watches, or any other form of technology, are not allowed in any School of Science testing situation (tests, quizzes, exams, etc.) whether the technology is being used or not to obtain answers. Students must place all technology and devices (must be in silent mode or powered off) in their closed bags placed under their chair. Students observed with any technology device may face penalties including failure of the test/quiz/exam/course, and the incident may be formally reported to the Dean of Students. Software S-Plus, SAS and R packages (available at www.R-project.org)

HOMEWORK Daily homework is assigned in class. Homework will not be collected and graded. Completing all homework sets on time is absolutely essential in learning the material and getting ready for quizzes and exams.

QUIZZES are given at the end of the quiz day for about 10 minutes (from 5:35-:45PM) and are based on homework problems due that day. The quizzes will be closed book and closed notes. Each of the 12 quizzes is worth 20 points (4%). There will be absolutely no make-up quizzes. Your lowest two quiz scores will be dropped. All quizzes together accounts for 200 points (40%).

Exams There will be three closed-book exams (one sheet of formulas permitted) in this course based on materials covered up to the previous class day. Each exam is for 75 minutes and worth 100 points (20%). There will be no make-up exams. No exam score will be dropped. The third exam is the final exam. However, MS (Applied/Bio Statistics) and PhD (Biostatistics and Mathematics) students are required to take a closed-book comprehensive exam on materials of STAT 51900 and 52800.

GRADING The percentage point distribution will be as follows: Top ten of twelve Quizzes (200 points), Three Exams (300 points). There will NOT be any make-up. Your letter grade will be determined by referring your achieved percentage score to the following absolute scale:

$$A \ge 90\% > B \ge 80\% > C \ge 70\% > D \ge 60\% > F$$

with "+" and "-" attached for scores falling in the upper and lower third of the range, respectively. I reserve the right to make adjustments to the overall grading policy, but the letter grade cutoffs will be no stricter than those advertised above. The letter grades given on Canvas are not based on above and hence not your final grades.

STUDENT CONDUCT Please refer to IUPUI Code of Student Rights, Responsibilities, and Conduct (http://studentcode.iu.edu/).

INCOMPLETES Grades of Incomplete will only be given in accordance with the university policy (http://www.registrar.iupui.edu/incomp.html). In particular, an incomplete cannot be given to a student who is not passing the course for whatever reason.

NO CLASS ATTENDANCE WITHOUT OFFICIAL ENROLLMENT After the conclusion of the 100% refund period (https://facultystaffcentral.iupui.edu/enrollment/index.html), all individuals attending classes on a regular basis MUST be officially enrolled in the class, attending the class based on formal arrangements to make up a prior grade of Incomplete, or enrolled as an auditor. One-time visitors to classes may be allowed only on an exception basis with prior permission of the instructor. This policy does not apply to individuals who provide assistance to a student with a documented disability, such as Adaptive Educational Services sign language interpreters, individuals who are involved in the course in an instructional role, or administrative personnel

## IMPORTANT DATES

Tues Jan 08 First day of class

Mon Jan 15 Martin Luther King Jr. Holiday-No class; All offices closed

Mon Mar 11 – Sun Mar 17 Spring Break Recess. No class

Mon Mar 18 Classes resume
Mon Apr 29 Last day of class
Fri April 26– Sun May 05 Final Exams

Friday, May 10 Final grades are available on transcripts at noon and

viewable through ONE (https://one.iu.edu.)

Table 1: Tentative Schedule

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Μ	Point estimates, Moment estimates, MVUE	Lec Notes	
W	M- and Z- estimates	Lec Notes	Quiz 1
W	M- and Z- estimates	Lec Notes	
$\mathbf{M}$	Maximum Likelihood Estimation	6.1 - 6.2	Quiz 2
W	C-R Lower Bound, Efficiency	6.2	
$\mathbf{M}$	Asymptotic normality	6.2	Quiz 3
W	Multi-parameter: Estimation	6.4	
$\mathbf{M}$	Multi-parameter: Estimation	6.4	Quiz 4
W	Exam 1		
$\mathbf{M}$	Hypothesis Testing	4.5	
W	Hypothesis Testing and Confidence Intervals	4.5	
$\mathbf{M}$	Chi-square test and Uni-parameter: LRT	4.7, 6.3, 8.3	Quiz 5
W	Likelihood Ratio Tests	6.5	
M	Sufficient statistics	7.2 - 7.3	Quiz 6
W	Sufficient statistics and its properties	7.2 - 7.4	
M	Property of Sufficiency Statistics	7.3 - 7.4	Quiz 7
W	Completeness, Uniqueness and Exponential Family	7.4-7.8	
$\mathbf{M}$	Exponential Family	7.5 - 7.6	Quiz 8
W	Comp-Uniq-Independence and Optimal Tests	7.9, 8.1	
M	Exam 2		
W	Most powerful tests	8.1	
M	Best critical regions	8.1	Quiz 9
W	Uniformly most powerful tests	8.1	
$\mathbf{M}$	Monotone likelihood ratio	8.2	Quiz 10
W	One-way ANOVA	9.1-2	
M	General estimating equations	Lec Notes	Quiz 11
W	ASN for GEE	Lec Notes	
$\mathbf{M}$	ASN for LSE	Lec Notes	Quiz 12
W	ASN for LSE	Lec Notes	
Μ	Exam 3		
	W W M W M W M W M W M W M W M W M W M W	M Point estimates, Moment estimates, MVUE W M- and Z- estimates W M- and Z- estimates M Maximum Likelihood Estimation W C-R Lower Bound, Efficiency M Asymptotic normality W Multi-parameter: Estimation M Multi-parameter: Estimation W Exam 1 M Hypothesis Testing W Hypothesis Testing and Confidence Intervals M Chi-square test and Uni-parameter: LRT W Likelihood Ratio Tests M Sufficient statistics W Sufficient statistics W Sufficient statistics and its properties M Property of Sufficiency Statistics W Completeness, Uniqueness and Exponential Family M Exponential Family W Comp-Uniq-Independence and Optimal Tests M Exam 2 W Most powerful tests M Best critical regions W Uniformly most powerful tests M Monotone likelihood ratio W One-way ANOVA M General estimating equations W ASN for GEE M ASN for LSE W ASN for LSE	WPoint estimates, Moment estimates, MVUELec NotesWM- and Z- estimatesLec NotesWM- and Z- estimatesLec NotesMMaximum Likelihood Estimation6.1-6.2WC-R Lower Bound, Efficiency6.2MAsymptotic normality6.2WMulti-parameter: Estimation6.4MMulti-parameter: Estimation4.5WExam 14.5MHypothesis Testing and Confidence Intervals4.5MChi-square test and Uni-parameter: LRT4.7, 6.3, 8.3WLikelihood Ratio Tests6.5MSufficient statistics7.2-7.3WSufficient statistics and its properties7.2-7.4MProperty of Sufficiency Statistics7.3-7.4WCompleteness, Uniqueness and Exponential Family7.4-7.8MExponential Family7.5-7.6WComp-Uniq-Independence and Optimal Tests7.9, 8.1MExam 28.1WMost powerful tests8.1MBest critical regions8.1WUniformly most powerful tests8.1MMonotone likelihood ratio8.2WOne-way ANOVA9.1-2MGeneral estimating equationsLec NotesWASN for LSELec NotesWASN for LSELec Notes