NORMAL WEIGHTED COMPOSITION OPERATORS ON THE HARDY SPACE

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ABSTRACT. Let ϕ be an analytic selfmap of the open unit disc \mathbb{U} and let ψ be an analytic function on \mathbb{U} such that the weighted composition operator $W_{\psi,\phi}$ defined by $W_{\psi,\phi}f = \psi f \circ \phi$ is bounded on the Hardy space $H^2(\mathbb{U})$.

In this talk we present a characterization of weighted composition operators that are unitary, showing that in contrast to the unweighted case, every automorphism of \mathbb{U} induces a unitary weighted composition operator. A conjugation argument, using these unitary operators, allows us to describe of all normal weighted composition operators for which the inducing map ϕ fixes a point in \mathbb{U} . In general, we show that if $W_{\psi,\phi}$ is normal, then ϕ must be univalent and ψ must be nonzero at each point of \mathbb{U} . Descriptions of spectra are provided for the operator $W_{\psi,\phi}$ when it is unitary or when it is normal and ϕ fixes a point in \mathbb{U} .

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