## Homework S2

1. Do problems $2,3,4,7,9,10$, and 12 on page 191 of the text.
2. Do problems $8,12,14,17$, and 21 on pages 194 and 195 of the text.
3. We proved (Theorem 4.7, page 187) that if $f$ is differentiable on an interval and $f^{\prime}(x)>0$ for every $x$ in the interval, then $f$ is strictly increasing on the interval.
(a) Prove: If $f$ is differentiable on the interval $(a, b)$ and $f^{\prime}(x) \geq 0$ for all $x$ with $a<x<b$ and $f^{\prime}(x)=0$ for at most one value of $x$ in $(a, b)$, then $f$ is strictly increasing in the interval $(a, b)$.
(b) What if there are exactly two points in the interval $(a, b)$ for which $f^{\prime}(x)=0$ ? (That is, either prove the same result as in part (a), or find an example with $f^{\prime}(x)=0$ exactly two times for which $f$ is not strictly increasing on $(a, b)$.)
