## Math 35100: Elementary Linear Algebra (Class No: 15781)

Prerequisite: Math 17100
Meets: MW 4:30-5:45p in IT 069
Final Exam: Monday, December 19, 3:30-5:30p (!)
Instructor: Carl Cowen
Office: LD 224P
Phone: 278-8846
Office Hours: M 3:00-4:00p, Tu 4:00-5:00p, W 1:00-2:00p, or by appointment
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Linear algebra is second only to calculus in terms of importance for applications. In many applications, the problem is formulated mathematically, it is then converted to a linear algebra problem (possibly without the user knowing it), the linear algebra problem is solved using a computer, and, finally, the results are interpreted. For example, many numerical routines for solving differential equations change the problem into a linear algebra problem first.

This is a mathematics course: We will develop the mathematics with theorems and their proofs. Throughout the course, we will remain conscious of the reliance on computers for real world computation, and there will be a formal computer component to the course. Most homework and test questions will be designed for paper and pencil computation, but you will be permitted (encouraged!!) to do your homework using a machine. You will be able to use Matlab software, capable of doing all the numerical computations required for the course, on many of the UITS machines on the IUPUI campus, including the labs on the second floor of LD and the first floor of IT. (GNU Octave is a free(!) numerical linear algebra package very similar to Matlab.) It is planned that the second midterm test and the final exam will be held in a computer laboratory so that you will be able to use Matlab software if you wish. The importance of computer computation will affect the development of some of the topics for the course. In many situations in linear algebra, the obvious method is not the one used in practice because it is too prone to error or too time consuming. We will always try to indicate the practical algorithms for solving linear algebra problems, and one of the goals of the course is to make it possible for you to understand the techniques used in linear algebra software, and read the documentation for such software.

The official text will be
Elementary Linear Algebra, by Howard Anton, 10th edition, Wiley (ISBN 978-0-470-45821-1)
An alternate text will be
Introduction to Matrix Analysis for Engineering and Science, by Carl Cowen (ISBN 0-9650717-6-6)
Reserve books in the library covering the topics of the course are both of the texts and also:
Introduction to Linear Algebra, by Gilbert Strang
Note: In this class, the homework assignments will be printed and handed out in class, and posted on the course web page, so it will not be necessary to purchase any text for the sole purpose of gaining access to the homework assignments.

There will be two midterm tests, each counting about $20 \%$ of your grade, and about $40 \%$ of your grade will come from the two-hour final exam scheduled for December 19. The first of the midterm tests will be a pencil and paper test lasting 70 minutes. If possible, the second midterm test and the final exam will be held in the computer lab, with 1.5 hours for the midterm and 2 hours for the final exam.

Weekly homework, class participation, and occasional quizzes will make up the remaining $20 \%$ of your grade. Make-up/late homework will not be graded for credit. Quizzes based on the homework will be announced in advance and will be the done the last ten minutes or so of the class. No make-up/late quizzes will be graded for credit; the lowest quiz grade will be dropped, with missed quizzes counted as zeros.

Unlike most mathematics classes, we will be using a classroom response device, a 'clicker', in class both for formal (i.e. graded) and informal (i.e. ungraded) responses. The data from the response devices will constitute the class participation part of your grade. We will use Turning Technologies ResponseCard RF LCD, one of the IUPUI standard devices, available at the bookstore for a little less than $\$ 50$. This is the same as the devices used in Chemistry and Physics classes in the School of Science. As I understand it, there are other responseware devices that can also be used with this system, such as some cellphones and some other handheld or laptop devices, and these can be licensed for a somewhat lower fee. More information about ResponseCards and responseware licenses is available at the webpage kb.iu.edu/data/ayps.html

An approximate syllabus is included below, but the developing schedule for the course will be announced in class and will also be on the website for the course, updated regularly.

You should show your all your work on homework and tests. Results of machine computations will be acceptable in all homework problems in place of hand computation; "show your work" in this case means writing down the computation you asked the machine to do and giving the result of this computation. (You should NOT!! attach a printout of your computer session!) Of course, justification and explanation of your computational work as well as proofs and your work on similar exercises will need to be written in the usual way.

My goals for you in this course are
Short term goal: That you master the ideas and computations of the course, both theoretical and applied.
Short term goal: That you become proficient in the language of linear algebra, as it is used both formally and informally in theoretical discussions and applications to problems from other disciplines.
Short term goal: That you develop your ability to read mathematics and learn from what you read.
Short term goal: That you develop your ability to write mathematics, and begin to develop your skill in creating and writing proofs, which are the explanations of why things in mathematics are true.
Long term goal: That you develop and sustain an excitement about mathematics and its connections to problems in the 'real world' generally, especially the mathematics you need in your professional and personal life, and that you can and do communicate that excitement to others.

## General Academic Policies

There are a number of campus-wide policies governing the conduct of courses at IUPUI. These can be found at http://registrar.iupui.edu/course_policies.html

The work you submit for homework, quizzes, tests, and the final exam must be your own. For homework you will probably find it beneficial to consult with other students about the material and this kind of conversation and collaboration is encouraged. At the end of the consultation, however, each participant is expected to prepare their own summary of the discussion and their own solutions to the problems. The policies for this class will be those derived from IUPUI's policies on academic conduct and adaptive services. More information about student conduct can be found at
http://registrar.iupui.edu/misconduct.html
More information concerning adaptive services for learning or other disabilities at IUPUI can be found at http://life.iupui.edu/aes/

## Some Important Dates

Date
August $22 \quad$ First Day of Classes
October 16 Last day to withdraw with adviser's signature and automatic "W"
October 17-18
October Break!! no classes
November 15
December 12
Last day to withdraw with permission of adviser and instructor
December 19

## Approximate Course Outline

Section numbers refer to the official text (Anton) and the alternate text (Cowen)
Anton Cowen Topic Lectures
1.3,4,7 $\quad 1.2,3 \quad$ Matrix algebra, special types of matrices ..... 1
4.2,9,10 $\quad 1.3 \quad$ Linear transformations, matrix multiplication as transformation ..... 1
$1.1 \quad 2.2 \quad$ Systems of linear equations ..... 1
$1.2 \quad 2.3 \quad$ Gaussian elimination ..... 1
$\begin{array}{lll}1.5 & 2.4 & \text { Inverses }\end{array}$ ..... 1
2.1-2.3 $2.6 \quad$ Determinants ..... 1
3.1,4, $3.2,3$ Euclidean spaces, real vector spaces, and subspaces,
4.1,2 linear combinations, spanning ..... 1
$4.3 \quad 3.4 \quad$ Linear independence ..... 1
$4.4 \quad 3.5 \quad$ Basis ..... 2
$4.5 \quad 3.6 \quad$ Dimension ..... 1
4.7,8 $\quad 3.7,8 \quad$ Rank-Nullity Theorem ..... 2
6.1,2 $4.2 \quad$ Inner products ..... 1
$6.3 \quad 4.3 \quad$ Gram-Schmidt algorithm ..... 1
4.4 Orthogonal complements and duality ..... 2
4.5 Matlab commands 'orth' and 'null' ..... 1
$\begin{array}{lll}6.4 & 5.2 & \text { Inconsistent systems }\end{array}$ ..... 1
$6.5 \quad 5.3$ Least squares fitting of data ..... 1

## Midterm Test II

(early November, probably in computer lab)
5.1 $\quad 6.2 \quad$ Eigenvalues and eigenvectors ..... 2
(5.4) $\quad(6.3,4) \quad$ Systems of differential equations (if time permits) ..... (?)
$5.2 \quad 6.5 \quad$ Similarity and diagonalization ..... 2
(6.6) Matrix exponential (if time permits) ..... (?)
7.1,2,5 $\quad 7.1 \quad$ Hermitian matrices ..... 2
Review ..... 1

## Final Exam

(Monday, December 19, 3:30p - 5:30p, probably in computer lab)

